

Example 1:

$$2x + 3y = 6$$

$$x + 4y = 13 \Rightarrow x = -4y + 13$$

$$\begin{aligned} 2x + 3y &= 6 \\ 2(-4y + 13) + 3y &= 6 \\ -8y + 26 + 3y &= 6 \\ -5y + 26 &= 6 \\ -5y &= -20 \\ y &= 4 \end{aligned}$$

$$\begin{aligned} x &= -4(4) + 13 \\ x &= -16 + 13 \\ x &= -3 \end{aligned}$$

$(-3, 4)$  is  
the solution

## **Watch Substitution Video**

**<http://www.shmoop.com/video/solving-systems-of-equations-by-substitution>**

Example 2:

$$\textcircled{y} - 5 = -3x \Rightarrow y = -3x + 5$$

$$7x + 3y = 7$$

$$7x + 3y = 7$$

$$7x + 3(-3x + 5) = 7$$

$$7x - 9x + 15 = 7$$

$$-2x + 15 = 7$$

$$-2x = -8$$

$$x = 4$$

$$y = -3(4) + 5$$

$$y = -12 + 5$$

$$y = -7$$

$(4, -7)$  is  
the solution



Example 3:

Solve by Substitution:

$$4x + 5y = 10$$

$$2x - 3y = 4 \Rightarrow 2x = 3y + 4 \Rightarrow x = \frac{3}{2}y + 2$$

$$4x + 5y = 10$$

$$4\left(\frac{3}{2}y + 2\right) + 5y = 10$$

$$6y + 8 + 5y = 10$$

$$11y + 8 = 10$$

$$11y = 2$$

$$y = \frac{2}{11}$$

$$x = \frac{3}{2}\left(\frac{2}{11}\right) + 2$$

$$x = \frac{3}{11} + 2$$

$$x = 2\frac{3}{11}$$

$$x = \frac{25}{11}$$

$\left(\frac{25}{11}, \frac{2}{11}\right)$  is the solution



Which methods are correct using substitution?

A.  $2x + y = 4$        $y = -2x + 4$   
 $-x + y = 1$        $-x + (-2x + 4) = 1$       yes

B.  $2x + y = 4$        $y = x + 1$   
 $-x + y = 1$        $2x + (x + 1) = 4$       yes

C.  $2x + y = 4$        $-x = -y + 1$   
 $-x + y = 1$        $-1(-x = -y + 1)$   
    $x = y - 1$   
 $2(y - 1) + y = 4$       yes

## You Try!

### Example 4:

$$-2y + x = -19 \Rightarrow x = 2y - 19$$

$$5x + 2y = 1$$

$$5x + 2y = 1$$

$$5(2y - 19) + 2y = 1$$

$$10y - 95 + 2y = 1$$

$$12y - 95 = 1$$

$$12y = 96$$

$$y = 8$$

$$x = 2(8) - 19$$

$$x = 16 - 19$$

$$x = -3$$

$(-3, 8)$  is the solution