

1) Write 3×10^5 in standard form.

$300,000$

8.EE.3

2) Is $\sqrt{23}$ a rational or an irrational number?

does not end or repeat

8.NS.1

3) Is a triangle with sides that measure 6 inches, 8 inches, and 9 inches a right triangle?

3, 4, 5
6, 8, 10

$$a^2 + b^2 = c^2$$
$$6^2 + 8^2 = 9^2$$
$$36 + 64 = 81$$

8.G.6
Not a rt. Δ . $100 \neq 81$

4) Tran had \$40.00 saved for a new bike. Four weeks later he had saved \$68.00. At what rate of change did

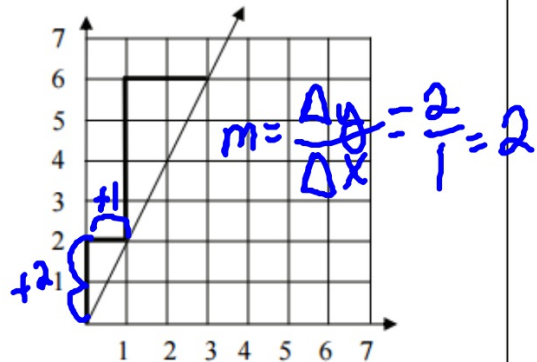
Tran's savings grow?

$(0, 40)$
 $(4, 68)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{68 - 40}{4 - 0} = \frac{28}{4} = 7$$

$\$7$ per week

5) What is the slope of the line in the coordinate plane?



Similarity



In the unit video, you saw examples of scale drawings and prototypes. Why is it important to create a scale drawing and prototype (or scale model) of a bridge, product, or sculpture design? How do you know that a prototype will accurately represent the end product?

Think about whether a product is the exact same size as or congruent to its prototype. Are there similarities

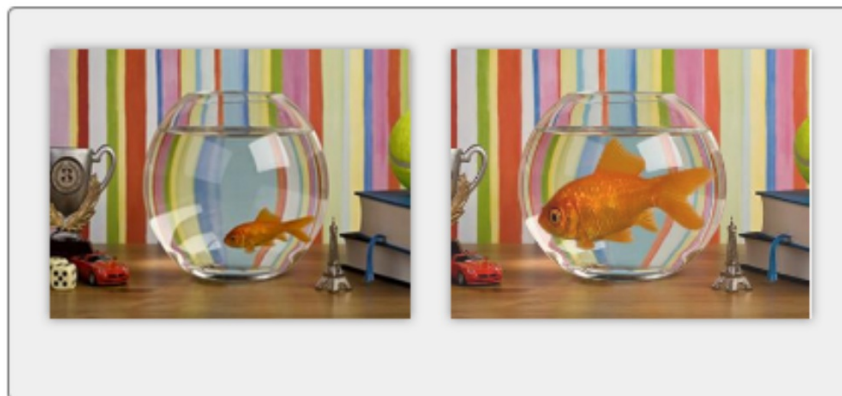
Which of the following properties of a two-dimensional figure are preserved under dilations?

- A.** measure of an angle
- B.** length of a line segment
- C.** perimeter of the figure
- D.** location of the figure
- E.** horizontal orientation of line segments
- F.** vertical orientation of line segments

The Right Moves

We discovered that dilations preserve the shape of a figure in the plane. Rigid transformations preserve shape. What do you think will happen to a figure if you apply a sequence of transformations, translations, rotations, reflections, or dilations?

Remember, when a figure can be expressed as the image of another under a series of rigid transformations, the figures are congruent. When a figure can be expressed as the image of another under a series of rigid transformations and *dilations*, the figures are said to be similar.



Determine whether each statement is true or false? Circle true or false.

A. Two triangles are similar if one triangle can be mapped onto the other through a sequence of transformations, including dilations.

True False

B. Two triangles are similar if two pairs of corresponding angles are equal.

True False

C. Two triangles are similar if they share a common vertex.

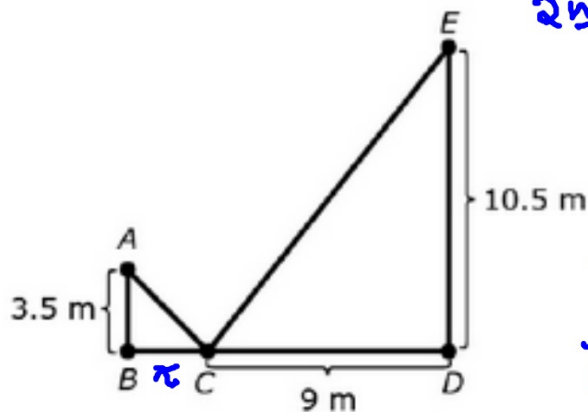
True False

In this figure, $\triangle ABC$ is similar to $\triangle EDC$.

$$\frac{AB}{BC} = \frac{ED}{DC}$$

$$\frac{3.5}{x} = \frac{10.5}{9}$$

$$x = 3$$



2nd way

$$\frac{3.5}{x} = \frac{10.5}{9}$$

$$10.5x = 31.5$$

$$\frac{10.5x}{10.5} = \frac{31.5}{10.5}$$

$$x = 3$$

What is the length, in meters, of \overline{BC} ? 3 meters

mary

ons

concept, you worked with **dilations**, which are transformations that can enlarge or reduce figures i

A **dilation** is a non-rigid transformation in which a figure is enlarged or reduced by a gi
factor around a given center point.

are reductions or enlargements based on a **scale factor** around a center of **dilation**.

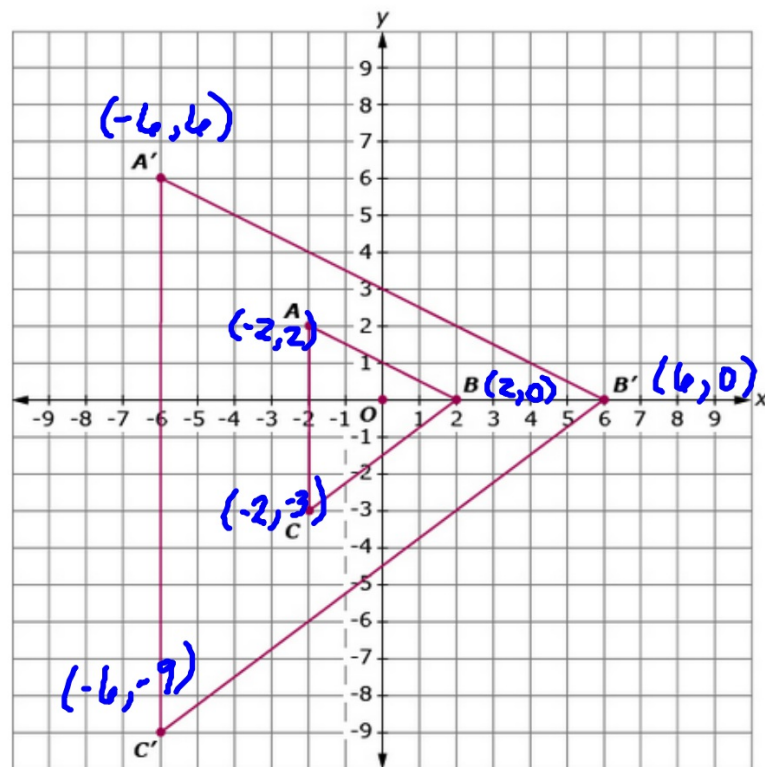
The scale factor is the ratio used to enlarge or reduce a pre-image to construct an image denoted by k *primes*.

The center of **dilation** is a fixed point in the plane about which the points in a figure are enlarged or reduced.

To determine the scale factor of a dilation, calculate the ratio of the length of a line segment in the image to the length of the corresponding segment in the pre-image.

Example 1: Dilation

Dilate triangle ABC by a scale factor of 3 around the origin.



Figures

s are **similar** if the ratios of their corresponding sides are equal and corresponding angles have the same measure.

Two figures that have the same shape and corresponding sides are proportional to each other are **similar**.

Using Similarity and Congruence in Terms of Transformations

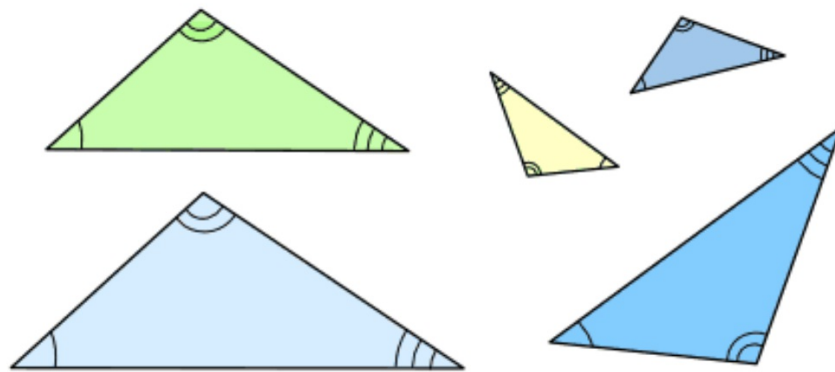
If a dilation has a scale factor $\frac{1}{1}$, the figures are congruent. Two figures are congruent if there is a sequence of rigid motion transformations that maps one to the other. All congruent figures are similar.

Two figures are similar if there is a sequence of rigid motion transformations and a dilation that maps one to the other.

Similar Triangles

triangles are **Similar** if the only difference is size (and possibly the need to turn or flip one around).

These triangles are all similar:



(Equal angles have been marked with the same number of arcs)

Some of them have different sizes and some of them have been turned or flipped.

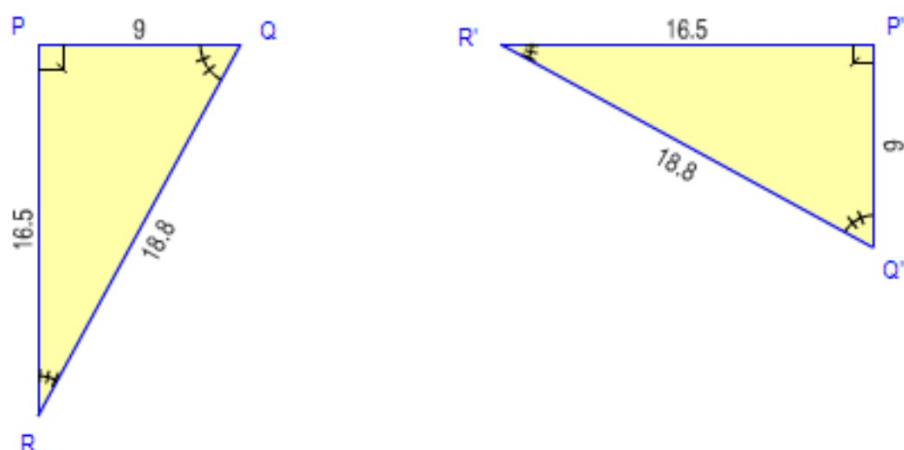
Similar triangles have:

- all their ^{corresponding} angles equal
- corresponding sides have the same ratio

Rotation

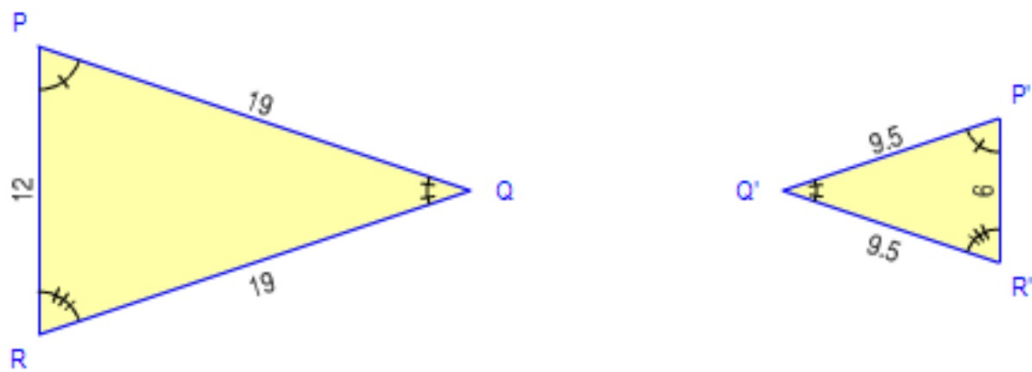
One triangle can be rotated, but as long as they are the same shape, the triangles are still similar. In the figure below, the triangle PQR is similar to P'Q'R' even though the latter is rotated clockwise 90° .

In this particular example, the triangles are the same size, so they are also **congruent**.



Conclusion

One triangle can be a mirror image of the other, but as long as they are the same shape, the angles are still similar. It can be reflected in any direction, up down, left, right. In the figure above, triangle PQR is a mirror image of P'Q'R', but is still considered similar to it.



present Similarity with Proportions: Investigation 1

Determine whether each statement is true or false? *Circle true or false.*

- A.** Side lengths of a figure are increased or decreased in proportion to the scale factor under a dilation.

True False

- B.** The measure of angles of a figure does not change under a dilation.

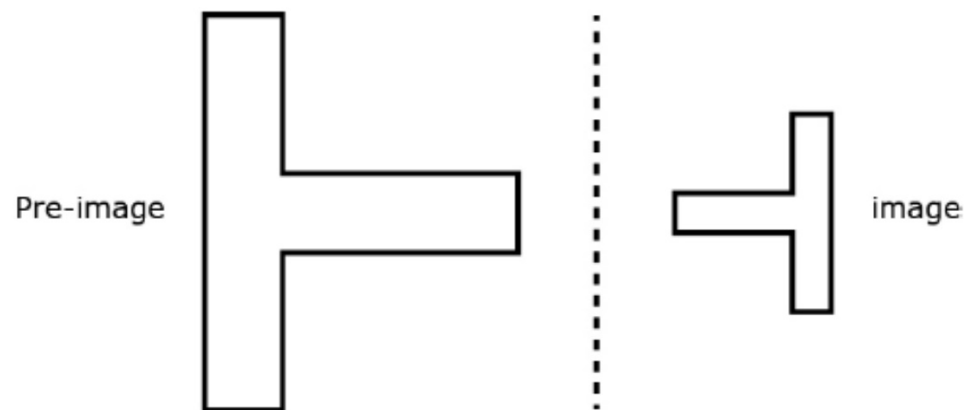
True False

- C.** A scale factor less than 1 for a dilation can be used to create an enlargement.

True False

reduction

2. Two similar figures are shown.



Which describes the sequence of transformations that maps the pre-image to the image?

- A. translation then dilation
- C. translation then rotation

- B. reflection then dilation**
- D. reflection then rotation

rectangle with a length of 12 centimeters is dilated to form a rectangle with a length of 3 centimeters. Which scale factor gives the ratio of the image to the pre-image?

A. 4

B. 3

C. $\frac{1}{3}$

D. $\frac{1}{4}$

Explain the difference between dilations and the other transformations that you have studied.

Dilations are non-rigid transformations that change the size of the original shape by a scale factor.

**Homework:
Check for Understanding
Worksheet**